

## Summer Math Packet: 7<sup>th</sup> to 8<sup>th</sup> Grade

Dear Students and Parents,

This summer, we encourage you to continue to practice your mathematics at home. Practicing math skills over the summer can keep the brain's pathways for computation and mathematical vocabulary strong.

Please make sure to follow the suggested directions for the best outcomes:

1. **Do NOT use a calculator (unless specified).** Take time to "grow your brain" and practice your math facts.
2. **Show all work!** An important aspect of mathematics is being able to communicate the process you use to arrive at your answer. It also provides an opportunity to review your thinking when making corrections to your work.
3. **Be neat and organized!** Part of success in math is being able to organize your work and keep track of your calculations and steps. Use all the paper you need to neatly show your work.
4. **Box your final answers** (another organizational strategy).
5. **Do not rush!** Take advantage of the summer pace and see if you digest more of what you're working on.
6. **If you are stuck on a problem, read the example problems provided at the beginning of each exercise.** If you are still stuck, check out one of the math websites listed below.
7. **Check your work!** If you got an incorrect answer, go back and try to figure out your error. Correcting your work and figuring out where you went wrong is monumental in the learning process.

Resources:

For help with a topic: [www.purplemath.com](http://www.purplemath.com) and select 7<sup>th</sup> grade on the left hand column, then select the topic from the top.

For Math Fact Practice: [www.aplusmath.com](http://www.aplusmath.com) and select flash cards. You can switch the operation and difficulty each time.

Another resource for help relearning a topic: [www.khanacademy.org](http://www.khanacademy.org)

Math Learning Games: [www.funbrain.com](http://www.funbrain.com)

Another suggestion: If you or your child has a cellular phone, there are free math apps that you can play on and build math skills. There are many out there. Try one out!

## Decimal Operations

1.  $9.372 + 3.029$

2.  $11.322 - 3.825$

3.  $18.23 - 5.409 + 2.55$

4.  $2.35 * 7.11$

5.  $1.023 * 3.5$

6.  $23.25 \div 0.7$

7.  $0.54723 \div 2$

8.  $8.752 \div 0.12$

For #9-12 simplify the fraction by finding common factors & eliminating them.

9.  $\frac{4}{10}$

10.  $\frac{24}{40}$

11.  $\frac{81}{27}$

12.  $\frac{9}{21}$

For #13-16, simplify each answer as much as possible by cross cancelling factors.

13.  $\frac{4}{5} * \frac{10}{18}$

14.  $\frac{8}{9} * \frac{3}{4} * \frac{10}{6} * \frac{12}{15}$

15.  $\frac{27}{38} \div \frac{3}{7}$

16.  $\frac{35}{38} \div \frac{5}{19}$

## Order of Operations

Simplify each expression using PEMDAS!

1)  $2 * 6 \div 4 + 7 - 8 * 3 + 77 \div 11$

4)  $13 + 2x - 5 - 8x + 7 * (4x + 1)$

2)  $72 \div 12 + 2^2 - 5 * 2 + 3 + 2 * (6 - 5)$

5)  $-5x - 8 + (8 \div 2) + 7 * 6$

3)  $7 * (12 - 5) + 9 \div (-3) + 7 * (-2)$

6)  $3x - 6 + 4 * 8 - 3x + 2y - 90 \div 5$

## Absolute Values & Negative Integer Operations

Simplify each statement as much as possible.

1.  $|-4|$

2.  $-|-5|$

3.  $(-3)^2$

4.  $-5^3$

5.  $-4 * 5$

6.  $-7 + 3$

7.  $-8 * -7$

8.  $-28 \div -7$

9.  $-42 + 27$

10.  $-22 - (-8)$

11.  $\frac{-42}{7}$

12.  $37 - 83$

13.  $-42 \div 2 + (7 * 3) + 8 - (-5) - 4 * 2$

14.  $|-2| + 8^2 - (-3)^2 + 7 * 2 - 22 \div 2$

15.  $|-4^3| - 8 * 7 + (-(-(-2)) + \left(-\frac{48}{6}\right) + (-3) * (-2)$

## Operations with Fractions

Reduce answers as much possible by finding common factors.

#1.  $\frac{2}{5} + \frac{3}{7}$

#2.  $\frac{4}{28} - \frac{7}{9}$

#3.  $3\frac{1}{3} + 4\frac{7}{8}$

#4.  $-\frac{7}{25} - \frac{8}{15}$

#5.  $\frac{2}{25} * \frac{15}{22}$

#6.  $\frac{27}{31} * -\frac{62}{81}$

#7.  $-\frac{10}{21} * -\frac{49}{35}$

#8.  $4\frac{1}{3} * 5\frac{2}{5}$

#9.  $-\frac{42}{55} \div \frac{28}{11}$

#10.  $\frac{25}{28} \div \frac{15}{32}$

#11.  $-\frac{8}{5} \div \frac{6}{35}$

#12.  $\frac{125}{128} \div \frac{65}{72}$

13. You have  $8\frac{4}{5}$  total cups of lemonade, and you want to share it with your friends. Each friend gets  $\frac{1}{10}$  of a cup to drink.  
How many friends do you have?

14. You have  $10\frac{2}{7}$  ounces of candle wax to make an army of tiny, beautiful-smelling candles. You are able to make a total of 12 candles from the wax. How much wax is in each candle? (Hint: write an equation first.)

## Exponents & Expressions

For #1-4, rewrite as multiplication problems, then solve.

#1.  $(-5)^4$

#2.  $\left(\frac{1}{2}\right)^3$

#3.  $-4^2$

#4.  $\left(-\frac{2}{3}\right)^3$

For #5-7, rewrite as exponents, and solve.

#5.  $2 * 2 * 2$

#6.  $\left(\frac{1}{4} * \frac{1}{4}\right)$

#7.  $-1 * -1 * -1 * -1 * -1 * -1 * -1$

Simplify the expression by combining terms.

#8.  $-2(x - 3) + 4x$

#9.  $4x - 1(6 + 2x)$

#10.  $4x - 3 + 6z + 7 - 10x$

#11.  $(6a + 3x) - (4a - 7x)$

#12.  $(-4y - 8x) + (7y + 10x)$

#13.  $(5x - 2a) - (-4x + 7a)$

#14.  $(15x - 3y) + (-12x - y)$

Find the greatest common factor of the following terms.

#15. 84, 128

#16.  $147x, 105x^2$

#17. 216, 288, 72

## Solving Equations

Solve each equation for the variable.

#1.  $2x + 6 = 8$

#2.  $-4(x - 2) = 16$

#3.  $\frac{x+7}{3} = 12$

#4.  $\frac{5x-3}{2} = 11$

#5.  $-3x - 7 = x + 9$

#6.  $4(2x + 6) = 16x + 8$

#7.  $2(x - 4) = 22$

#8.  $-5x = 35$

#9.  $\frac{x}{4} + 3 = 7$

#10.  $-\frac{2x}{5} = 10$

#11.  $-\frac{x-5}{2} = 11$

#12.  $\frac{2x+1}{2} = 3x$

Factor out any common factors from each expression.

#13.  $81x + 27$

#14.  $3x - 9$

#15.  $-48 - 64x$

## Inequalities

For #1-2, write a sentence that represents the inequality.

#1.  $x < 7$

#2.  $x \geq -4$

For #3-4, tell if the given number makes the inequality TRUE or FALSE.

#3.  $2x < 10$ , value =  $-3$

#4.  $\frac{x+7}{6} \geq -5$ , value =  $5$

Solve the inequalities, showing each step. Then graph the solutions.

#5.  $x + 7 \leq -2$

#6.  $\frac{3}{5}x > 9$

#7.  $7 - 2x \geq 5$

#8.  $-x - 8 < 3$

#9.  $-\frac{5}{6}x \geq 15$

#10.  $2x - 5 > 3x + 6$

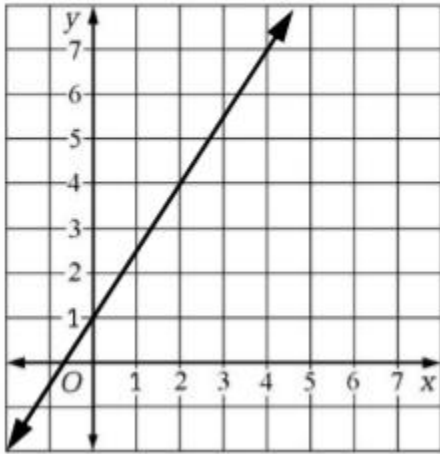
#11.  $3x - 8 < 3x + 7$

#12.  $3x + 7 > 4$

#13.  $-2x + 7 < 9x - 2$

## Coordinate Plane & Unit Rates

For #1-3, use the graph given to answer the questions.



#1. When  $x = -2$ , what is Y?

#2. When  $y = 4$ , what is X?

#3. When  $x = 4$ , what is Y?

For #4-6, use the equation  $y = -3x + 2$  to find the value of  $y$  at the given  $x$  values.

#4.  $x = 3$

#5.  $x = -\frac{5}{3}$

#6.  $x = 0$

#7.  $x = -4$

For #7-10, write the ratio as a fraction in its simplest form (reduce!).

#8. 56 to 77

#9. 144 to 84

#10. 15 to 45

#11. 36 : 108

Find the unit rate [by making the denominator 1].

#12.  $\frac{28 \text{ megabytes}}{5 \text{ seconds}}$

#13.  $\frac{45 \text{ cups of coffee}}{4 \text{ days}}$

#14.  $\frac{28 \text{ detentions}}{9 \text{ days}}$

## Proportions & Slope

For #1-3, tell if the statements are proportional. Show your work.

1.  $\frac{3}{7} = \frac{81}{189}$

2.  $\frac{22}{8} = \frac{152}{56}$

3.  $\frac{5}{6} = \frac{70}{82}$

For #4-6, write a proportion for the situation, and then solve.

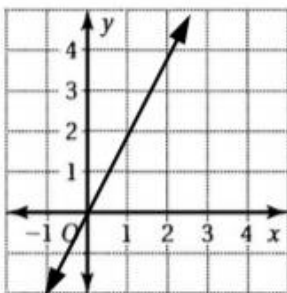
4. A test is worth 36 total points and you want to get an 87% on it. How many points do you need to score?

5. You pay \$4 for 7 pounds of chocolate frogs. How much would you pay for 11 pounds of chocolate frogs?

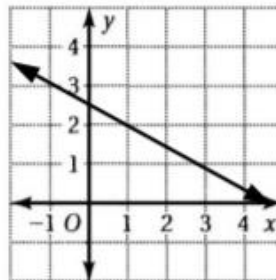
6. The ratio of chocolate to vanilla ice cream is 3 scoops to 7 scoops. If there are 147 scoops of vanilla ice cream, how many total scoops are there?

For #7-8, find the slopes of the graphs provided.

7.



8.



For #9-11, use the points given to find the slope between them. (Answers might be fractions!)

9.  $(-3, 4)$  and  $(-1, -2)$

10.  $(7, 9)$  and  $(2, -1)$

11.  $(-21, 9)$  and  $(19, -4)$

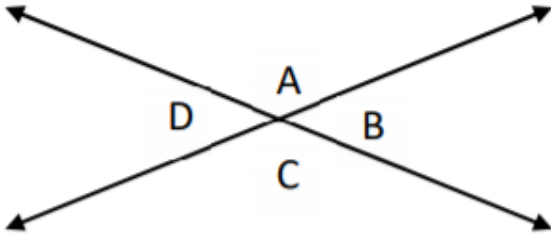
## Decimals, Fractions, Percents

1. Write 0.42 as a fraction.
2. Write  $\frac{7}{35}$  as a decimal.
3. Write 74% as a fraction.
4. Write 0.5732 as a percent.
5. Write  $\frac{3}{11}$  as a percent.
6. Write  $\frac{6}{25}$  as a percent.

**For #7-12, turn the sentences into equations, and solve.**

7. What number is 37% of 7?
8. 22% of 45 is what number?
9. 7 is 37% of what number?
10. What is 212% of 3?
11. 0.15% of 3,034 is what number?
12. 6 is 8% of what number?
13. A company makes a table for \$15 and sells it for \$19. What is the percentage of markup?

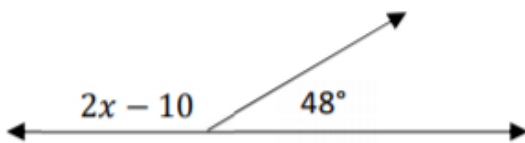
## ANGLES



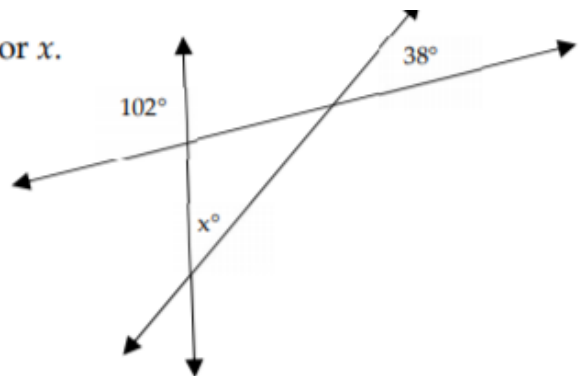
1. List the pairs of adjacent angles.
2. List the pairs of vertical (opposite) angles.

3. Angle Z and Angle X on intersecting lines are vertical angles. If Angle Z is  $63^\circ$ , what is Angle X?
4. Angle K and Angle J on intersecting lines are adjacent angles. If Angle K is  $105^\circ$ , what is angle J?
5. The total sum of **complementary** angles is \_\_\_\_\_.
6. The total sum of **supplementary** angles is \_\_\_\_\_.
7. Angle B and Angle C are **complementary**. If Angle B is  $43^\circ$ , what is Angle C?

8. Solve for  $x$ .



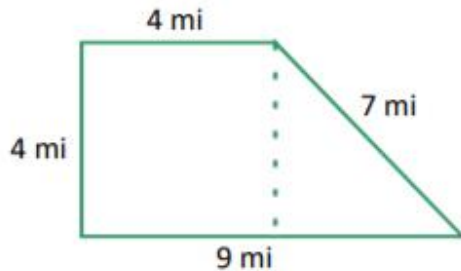
9. Solve for  $x$ .



## Area, Perimeter, and Circumference

1. A circle has a radius of 3 inches. A) What is the diameter? B) What is the area of the circle? C) What is the circumference of the circle?

2. A circle has a diameter of 8 meters. A) What is the radius? B) What is the area of the circle? C) What is the circumference of the circle?



3. What is the perimeter of the figure to the right?

4. What is the area of the figure to the right?

5. What is the area of a parallelogram with a base of **9 inches** and a height of 7.62 **centimeters**?

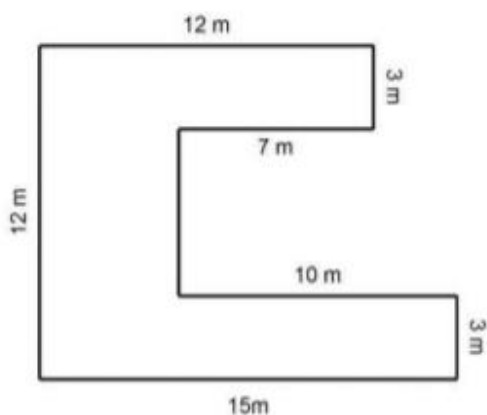
6. The area of a rectangle is  $58 \text{ in}^2$ . The base is 8 inches long. What is the height?

7. A circle has a circumference of  $14\pi$  inches. What is the diameter of the circle?

8. A triangle has an area of  $160 \text{ mi}^2$ , and a base of 20 miles. What is the height?

9. What is the area of a triangle that has a base of 8 meters and a height of 7 meters?

10. A circle has an area of  $49\pi \text{ m}^2$ . What is the radius of the circle?

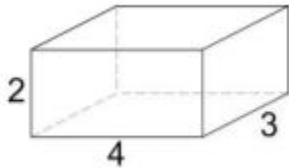


11. Find the perimeter of the shape to the left.

12. Find the area of the shape to the left.

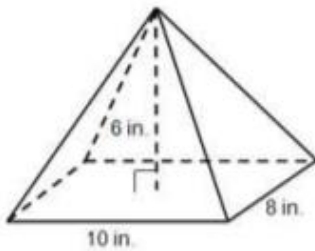
## Surface Area and Volume

1. A giant lobster tank is a **cylinder**. The base has a radius of 3 miles. It is 10 miles tall.  
A) What is the area of the base? B) What is the tank's volume? C) What is the surface area?

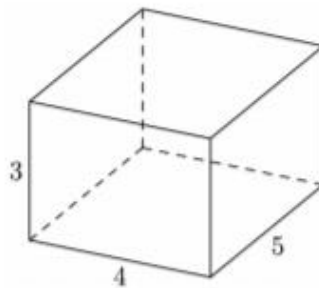


2. The shape to the left is measured in millimeters.  
A) What is the area of the base? B) Volume? C) Surface area?

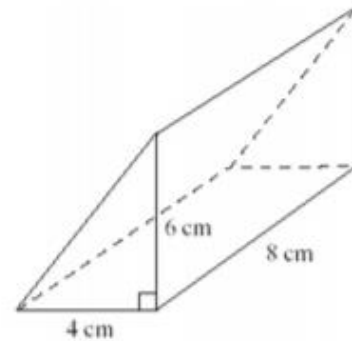
3. Find the volume.



4. Find the volume.



5. Find the volume.



6. A cylinder has a volume of  $80\pi \text{ in}^2$ . The radius is 4 inches! What is the cylinder's height?

7. A right **rectangular** prism has a surface area of  $180 \text{ m}^2$ . The perimeter of the base is 28 meters. The width of the base is 6 m and the length of the base is 8 m. What is the height of the prism?

## Probability

List A) the amount of events in each experiment, and B) the total amount of outcomes.

1. Rolling a 6-sided die 3 times
2. Flipping a coin 4 times
3. Filling 3 different positions with 7 different people
4. Making one meal from 3 appetizers, 5 main courses, 4 desserts, and 3 drinks

For 5-6, find the theoretical probability of the event.

5. Rolling two six-sided dice and getting a total of 7
6. Flipping 3 two-sided coins and getting two heads and a tail
7. You have a bag of lizards. There are 3 green lizards, 5 red lizards, 4 orange lizards, 6 white lizards, and 2 black lizards.
  - A) What is the theoretical probability of drawing a green lizard?
  - B) What is the theoretical probability of drawing an orange OR a white lizard?
8. You reach into the bag and draw 10 lizards, replacing them every time. You draw 4 red lizards, 2 white lizards, and 4 green lizards.
  - A) What is the **experimental** probability of drawing a green lizard?
  - B) Which is bigger, the theoretical or experimental probability of drawing a green lizard?
9. You're making cookies for a bake sale. The probability of frosting a good cookie is  $\frac{3}{7}$ . You frost 812 cookies. How many good cookies do you manage to frost?
10. You're harvesting Brussel sprouts. The chance of finding a yummy Brussel sprout is  $\frac{2}{27}$ . If you find 48 yummy Brussel sprouts, what is the total amount of Brussel sprouts?

**p. 2 Decimal Operations**

- 12.401
- 7.497
- 15.371
- 16.7085
- 3.5805
- 33.2314
- 0.273615
- 72.933
- $\frac{2}{5}$
- $\frac{3}{5}$
- 3
- $\frac{3}{7}$
- $\frac{4}{9}$
- $\frac{8}{9}$
- $\frac{9}{4}$
- $\frac{7}{2}$

**p. 3 Order of Operations**

- 7
- 5
- 32
- $15+22x$
- $-1x+34$
- $8+2y$

**p. 4 Absolute Values & Negative Integer Operations**

- 4
- 5
- 9
- 125
- 20
- 4
- 56
- 4
- 15
- 14
- 6
- 46
- 5
- 60
- 4

**p. 5 Operations with Fractions**

- $\frac{29}{35}$
- $-\frac{40}{63}$
- $\frac{197}{24}$
- $-\frac{61}{75}$
- $\frac{3}{55}$
- $-\frac{2}{3}$
- $-\frac{2}{3}$
- $\frac{117}{5}$
- $-\frac{3}{5}$
- $\frac{40}{21}$
- $-\frac{28}{3}$
- $\frac{225}{208}$
- 88 friends  $[\frac{44}{5} \div \frac{1}{10}]$
- $\frac{6}{7}$ oz per candle  $[\frac{72}{7} = x \times 12]$

**p. 6 Exponents & Expressions**

- 625
- $\frac{1}{8}$
- 16
- $-\frac{8}{27}$
- $2^3 = 8$
- $(\frac{1}{4})^2 = \frac{1}{16}$
- $(-1)^7 = -1$
- $2x + 6$
- $2x - 6$
- $4 - 6x + 6z$
- $2a + 10x$
- $3y + 2x$
- $9x - 9a$
- $3x - 4y$
- 4
- $21x$
- 72

**p. 7 Solving Equations**

- $x = 1$
- $x = -2$

- $x = 29$
- $x = 5$
- $x = -4$
- $x = 2$
- $x = 15$
- $x = -7$
- $x = 16$
- $x = -25$
- $x = -17$
- $x = \frac{1}{4}$
- $27(3x + 1)$
- $3(x - 3)$
- $16(3 + 4x)$

**p. 8 Inequalities**

- X is less than 7
- X is more than or equal to -4
- Yes, -6 is less than 10
- Yes, 2 is more than -5
- $x \leq -9$
- $x > 15$
- $x \leq 1$
- $x > -11$
- $x \leq -18$
- $x < -11$
- All real numbers (true that  $-8 < 7$ )
- $x > -1$
- $x > \frac{9}{11}$

**p. 9 Coordinate Plane & Unit Rates**

- $y = -2$
- $x = 2$
- $y = 7$
- $y = -7$
- $y = 7$
- $y = 2$
- $y = 14$
- $\frac{8}{11}$
- $\frac{12}{7}$
- $\frac{1}{3}$
- $\frac{1}{3}$
- $5.6 \frac{\text{megabytes}}{\text{s}}$

13.  $11.25 \frac{\text{cups}}{\text{day}}$
14.  $3.11111 \frac{\text{detentions}}{\text{day}}$

**p. 10 Proportions & Slope**

1. Yes  $567=567$
2. No  $1232 \neq 1216$
3. No  $410 \neq 420$
4.  $\frac{x}{36} = \frac{87}{100}$  You need to get 31.32 points
5. \$6.29
6. 343 total scoops
7.  $m = 2$
8.  $m = -\frac{1}{2}$
9.  $m = -3$
10.  $m = 2$
11.  $m = -\frac{13}{40}$

**p. 11 Decimals, Fractions, Percents**

1.  $\frac{21}{50}$
2. 0.2
3.  $\frac{37}{50}$
4. 57.32%
5.  $0.\overline{27}$
6. 0.24
7. 2.59
8. 9.9
9. 18.919
10. 6.36
11. 455.1
12. 75
13. 26.67%

**p. 12 Angles**

1. AB, B/C, C/D, D/A
2. AC, DB
3.  $63^\circ$
4.  $75^\circ$
5.  $90^\circ$
6.  $180^\circ$
7. Angle B =  $43^\circ$ , Angle C =  $63^\circ$
8.  $71^\circ$
9.  $40^\circ$

**p. 13 Area, Perimeter, and Circumference**

1. A) 6 in B)  $9\pi \text{ in}^2$   
C)  $6\pi \text{ in}$
2. A) 4 m B)  $16\pi \text{ m}^2$  C)  $8\pi \text{ in}$
3. 24 mi
4.  $26 \text{ mi}^2$
5. 27 in
6. 7.25 in
7. 14 in
8. 16 mi
9.  $28 \text{ m}^2$
10. 7 m
11. 68 m
12.  $111 \text{ m}^2$

**p. 14 Surface Area and Volume**

1. A)  $9\pi \text{ mi}^2$  B)  $90\pi \text{ mi}^3$   
C)  $78\pi \text{ mi}^2$
2. A)  $12 \text{ mm}^2$  B)  $24 \text{ mm}^2$   
C)  $52 \text{ mm}^2$
3.  $160 \text{ in}^3$
4.  $60 \text{ units}^3$
5.  $96 \text{ in}^3$
6. 5 in
7. 3 m

**p. 15 Probability**

1. 3 events, 216 outcomes
2. 4 events, 16 outcomes
3. 3 events, 5040 outcomes  
( $7 \times 6 \times 5 \times 4 \times 3 \times 2 \times 1$ )
4. 1 event, 180 outcomes  
( $3 \times 5 \times 4 \times 3$ )
5.  $\frac{1}{6}$
6.  $\frac{3}{8}$
7. A)  $\frac{3}{20}$  B)  $\frac{1}{2}$
8. A)  $\frac{2}{5}$  B) Experimental
9. 348 [ $\frac{3}{7} = \frac{x}{812}$ ]
10. 648 [ $\frac{2}{27} = \frac{48}{x}$ ]